A novel three-dimensional numerical model for PV/T water system in hot climate region

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These two authors contributed equally to this research.
Graphical abstract
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Abstract

Hybrid PV/Thermal systems (PV/T) are proposed to harvest the two renewable forms of solar energy, electrical and thermal. The use of PV/T systems improves electrical efficiency while utilizing the available solar thermal energy for various heating applications. In this work, numerical simulations perform for PV/T system in hot climate conditions. The cooling system consists of eleven channels arranged in parallel to each other on the backside of the PV module. A novel three-dimensional numerical model of the PV/T system was developed to evaluate the thermal efficiency. The standard k – epsilon model was used to simulate the flow. This novel system was based on using symmetric-convection boundary conditions for the right and left sides of the PV/T model and symmetric-symmetric boundary conditions for the middle cooling channels rather than simulating the whole cooling system. Using one channel simulation allows the creation of less number of meshes, hence, reduces the computational time. The thermal efficiency was estimated by the superposition method for all cooling channels of the PV/T system. The thermal efficiency of the PV/T system was 60% at 0.4 (L/min) and 68% at 5.4 (L/min). The obtained results were in good agreement with the results presented in the literature.

Keywords: PV/T; Novel numerical model; CFD model simulation; PV cooling; Hot climate
1. Introduction

The increased demand and consumption of fossil fuels led to their fast depletion along with the elevation of greenhouse gas emissions and consequently, global warming and climate change [1, 2]. The utilization of renewable energy resources and/or the implementation of co-generation approaches are some favorable alternatives to fossil fuel consumption [3]. Solar energy, in particular, is not like conventional energy resources that have high environmental impacts. It is a renewable, abundant, and green source for a sustainable future [4-7].

Hybrid PV – Thermal (PV/T) systems that combined photovoltaic (PV) solar cells with solar thermal absorbers showed significant enhancements in capturing solar energy [8]. Both electrical and thermal energies are harvested from solar radiation using PV/T hybrid systems. Hence, in addition to, enhance the electrical efficiency of PV cells, the hybrid system of PV/T will also capture the thermal energy that can be utilized in various heating applications [9]. This is mainly because the increase in the PV cell temperature reduces the efficiency of PV cells dramatically [10]. Nevertheless, the implementation of the PV/T system allows the user to utilize the thermal energy [11].

Several techniques were used for PV cooling such as forced water circulation, forced air circulation, water spraying, water immersion, heat sink, phase change materials, transparent cooling, and thermoelectric cooling [12]. Water and air are the most commonly utilized cooling fluid in PV/T systems [13], where the PV/T system is named according to the cooling fluid utilized. For instance, PV/T/w and PV/T/a are the water and air-cooled PV/T systems, respectively. The selection of cooling fluid depends on several aspects and conditions. Using air as the cooling fluid is simple and cheaper and consequently, more economically feasible.
However, it is not efficient in hot climates where air temperatures are above 20°C [14]. On the other hand, using water is more efficient, yet, the cooling system would be more expensive when compared to the air [15,16]. The utilization of a nanofluid instead of water in a PVT system improves the performance and further enhances both electrical and thermal efficiencies [17]. Illustratively, Nasrin et al. [18] performed experimental and numerical studies for the enhancement of the efficiency of the PV/T system using nanofluid based on water/MWCNT for different irradiation and MWCT weight fractions. Their results showed that the overall efficiency at 1000 W/m² irradiance was improved and reached up 89.2%. PV/T systems can be classified in accordance with the fluid utilized for cooling, heat extraction type, system configuration arrangement, solar input type, and end-use purpose. Figure 1 summarizes the various classification of PV/T systems [13].
Figure 1: Classification of PV/T systems [13].

United Arab Emirates (UAE) is located in the Arabian Peninsula which is recognized for the hot and sunny climate throughout the entire year [19]. This substantial exposure to solar radiation encourages the country to promote photovoltaic technology for electricity generation [20,21]. PV systems are more environmentally friendly compared to other renewable energy technologies with no significant operational pollution [22-24] and they require less operating and maintenance costs [25]. The UAE is one of the highest worldwide countries in electricity consumption, where the total annual electrical production for Abu Dhabi Water and Electricity Authority (ADWEA) and Dubai Water and Electricity Authority (DEWA) was approximately 123.0 TWh and the per capita consumption was around 13.1 MWh [26]. Despite the abundance of oil in UAE, the country's vision is to include renewable energy and nuclear energy in its energy mix [27]. The UAE is progressing substantially in achieving its goal by installing several solar power plants such as SHAMS solar power plant and Mohammed Bin Rashid solar park [28]. Nevertheless, the UAE hot and dusty weather depresses the performance of solar power systems. For instance, elevated temperatures [29,30], as well as the accumulation of dust [31,32], negatively affect the performance of various generations of PV cells. Consequently, the implementation of solar PV systems in UAE is problematic without proper cooling and cleaning.

Nowadays, the electrical efficiency of commercial PV panels ranges from 10 to 25 % [33]. This means 75 – 90 % of the solar radiation falls on a PV module is either reflected or dissipated as thermal energy. The latter leads to decreasing the open-circuit voltage and the fill factor of the module due to the increase in the PV module temperature, hence, decreases the PV module electrical efficiency [34]. Currently, the most employed PV cells are the monocrystalline silicon
(mono c-Si) and the polycrystalline Silicon (poly c-Si) [35]. The efficiencies of these types are strongly affected by the increase of the panel temperature [34-38], with a temperature coefficient between –0.45 and –0.50% [39]. However, the effect of temperature on the amorphous silicon cells is significantly lower, with a temperature coefficient of about –0.25% [40].

Numerous numerical and experimental research investigations have been performed recently to study, the effect of variation of temperature, irradiation, wind speed, and mass flow rate of the cooling fluid on the efficiencies of PV/T systems [41-44]. These studies focused mainly on the overall efficiency of the system, i.e. electrical and thermal efficiencies, and on identifying the PV/T system that possesses the best performance and the lowest cost. Few studies [43, 45-47] examined the use of the three-dimensional simulation for the whole PV/T system. The results of these studies revealed that the thermal efficiency seems to vary with the shape of the cooling collector, area of PV module, solar irradiance, fluid cooling temperature, overall heat transfer coefficient, specific heat, and mass flow rate of cooling fluid.

The novel numerical model used in this study is based on simulating one cooling channel instead of simulating the whole PV/T system as reported in other numerical simulations in the literature. The simulations were performed in this model three times, one time for a cooling channel in the middle of the PV/T system, one time for the channel on the left side, and one time for the channel on the right side of the PV/T system. This was achieved by applying symmetric-symmetric thermal boundary conditions for the channel in the middle and symmetric-convection thermal boundary conditions for the channels on the left and right sides. It is worthwhile to mention that the numerical simulations performed for the whole PV/T system require a very high number of elements and consume more computational time. For instance, the numbers of
elements used by Nasrin et al. [43], Pang et al. [45], and Misha et al. [46] were 1,434,582, 3,262,009, and 2,432,207, respectively. These are 5 to 12 times higher than the number of elements used in this study which was 270,000 elements with a computational time of only 7 minutes. This study aims at numerically studying the performance of a PV/T system using a novel three-dimensional model under real conditions of irradiance and temperature for Sharjah city, UAE as a semi-arid climate with hot summer and mild winter.

2. Methodology

2.1 Electrical part

The PV module based on polycrystalline silicon was used, the electrical features of this PV module are shown in [48]. The maximum power point \( P_{MPP} \) produced by a solar PV system is calculated by Eq. 1:

\[
\dot{Q}_{MPP} = P_{MPP} = I_{MPP}V_{MPP} = (FF)V_{oc}I_{sc}
\]  

(1)

where \( I_{MPP} \) and \( V_{MPP} \) are the current and the voltage at the maximum power point, respectively, and \( FF \) is the fill factor that varies from one cell to another. This variation is based on the quality of the material used in the cell (purity of silicon). Moreover, the open-circuit voltage and the short circuit current are \( V_{oc} \) and \( I_{sc} \), respectively. The electrical efficiency \( \eta_{elec} \) of the PV module is determined using Eq. 2:

\[
\eta_{elec} = \frac{I_{MPP}V_{MPP}}{GA}
\]  

(2)

where \( A \) is the area of the PV module (1.17 m × 0.67 m), and \( G \) is the irradiance or the solar radiation in (W/m\(^2\)). The value of \( MPP \) varies from one location to another based on the ambient
The effect of the temperature on the MPP is given by temperature coefficients for current, voltage, and power. The electrical characteristics of the PV module under different conditions are calculated based on the aforementioned coefficients and the electrical characteristics under standard test conditions (STC) of the PV module. However, the electrical efficiency of the PV module under the effect of the temperature is shown in Eq. 3 [34].

$$\eta_{elec} = \eta_{ref} \left[ 1 - \beta_{ref}(T - T_{ref}) \right]$$

(3)

where the $\eta_{ref}$ is the efficiency at reference temperature, $\beta_{ref}$ is the temperature coefficient for the electrical efficiency, $T$ is the temperature under actual operating condition (-40 – 85°C) and $T_{ref}$ is the reference temperature under STC (25°C). This drop in efficiency can be reduced by using a suitable cooling system to keep the solar module operating close to the SOC.

### 2.2 Thermal part

The rate of heat removal ($\dot{Q}_{th}$) by the cooling system can be calculated as follows:

$$\dot{Q}_{th} = \dot{m}_{water} C_p (T_{outlet} - T_{inlet})$$

(4)

where $\dot{m}_{water}$, $T_{outlet}$, $T_{inlet}$, and $C_p$ are the mass flow rate, outlet temperature, inlet temperature, and specific heat of the cooling water, respectively. The inlet temperatures were recorded at different values of irradiance and. Moreover, the rate of the useful thermal energy ($\dot{Q}_u$) is the difference between the rates of absorbed radiation and heat losses and is given by Eq. 5:

$$\dot{Q}_u = A_c \left[ G - U_e (T_{p,m} - T_a) \right]$$
where $A_c$ is the surface area of the collector, $U_L$ is the overall loss heat transfer coefficient, $T_{p,m}$, and $T_a$ are plate mean temperature and ambient temperature, respectively. However, because of the difficulty in measuring $T_{p,m}$, Eq. 5 was modified by Hottel and Wilhier [49] to be:

$$\dot{Q}_u = A_c F_R \left[ G - U_L (T_{p,m} - T_a) \right]$$

(6)

where $F_R$ is the removal factor and it varies with the incident solar radiation, collector shape design, and fluid operating condition as shown in Eq. 7:

$$F_R = \frac{m C_P}{A_c U_L} \left[ 1 - \frac{\left( \frac{\dot{m}_c U_L}{m C_P} \right)}{A_c U_L} \right]$$

(7)

Where $F'$ is the collector efficiency factor. Moreover, the thermal efficiency of the PV/T system ($\eta_{th}$) is calculated based on the rate of thermal energy extracted from the PV module as shown in Eq. 8:

$$\eta_{th} = \frac{\dot{Q}_{th}}{G A}$$

(8)

Finally, the overall efficiency is the sum of thermal efficiency and electrical efficiency of the PV/T system ($\eta_o$) and is calculated as follow:

$$\eta_o = \eta_{th} + \eta_{elec}$$

(9)
One way to improve the efficiency of the PV/T system is to couple it with other heat users such as driving a heat pump. This would convert solar energy into useful heat more efficiently and increase the working fluid temperature from the combined system significantly, hence, improve the overall utilization efficiency of solar energy [50]. However, the coupling adds to the complexity of the system and requires additional management due to the instability and intermittency nature of solar energy. For instance, during the summer season, the thermal energy produced from the combined system could be used to heat the domestic hot water supply, while during the winter season an auxiliary heater could be utilized to provide the desired thermal energy. Moreover, to attain a steady heating system, the system should be combined with a built-in thermal energy storage system such as a reversible thermochemical reaction or a phase change material [51]. However, adapting a thermal energy storage system raises the cost of the system and introduces more constraints for the system location, therefore, affects the feasibility of the whole system [52]. Furthermore, to obtain a more accurate estimate of the PV/T efficiency the calculations should be corrected by considering the effect of soiling, energy losses in wires and converters, and heat losses in the hydraulic loop [52].

2.3 Experimental setup and uncertainty

The PV/T system consists of a PV module and a thermal system, the specifications of these systems are presented in Table 1.

Table 1. PV/T system specifications.

<table>
<thead>
<tr>
<th>PV/T Components</th>
<th>Specification</th>
</tr>
</thead>
<tbody>
<tr>
<td>PV</td>
<td>Poly-crystalline Si</td>
</tr>
<tr>
<td>$P_{\text{max at STC}}$</td>
<td>100 W</td>
</tr>
</tbody>
</table>
The IV and power curves at different irradiance for the PV module were measured by PROFITESTPV. The thermal energy for PV/T system was calculated at different irradiance by measuring the mass flow and the inlet and outlet temperatures of the cooling channel as presented in Eq. 4. The relative uncertainty for electrical and thermal efficiency were both estimated based on the uncertainty associated with the measuring instruments used in the experimental setup as shown in Table 2. The absolute uncertainties for measurement parameters were estimated based on the instrument device uncertainty and the repetition uncertainty for the measured parameter as shown in Eq. 10.

\[
\delta p = \sqrt{(\delta p_{dev})^2 + (\delta p_{rep})^2}
\]  

where \(\delta p_{dev}\) and \(\delta p_{rep}\) are the device and repetition uncertainties for the measured parameter, respectively.
Table 2. Absolute uncertainties for the instrument device and the measured parameter

<table>
<thead>
<tr>
<th>Instrument device</th>
<th>Measurement variable</th>
<th>Uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td>PROFITESTPV</td>
<td>Solar irradiance</td>
<td>± 10 W/m² for (T_{cell} ± 1 K)</td>
</tr>
<tr>
<td>PROFITESTPV</td>
<td>Peak power</td>
<td>± 5 W</td>
</tr>
<tr>
<td>Thermocouple type K</td>
<td>Ambient temperature</td>
<td>± 0.5°C</td>
</tr>
<tr>
<td>TM700 Thermocouple</td>
<td>Cooling fluid temperature</td>
<td>0.1 to 0.3°C</td>
</tr>
<tr>
<td>VYAIR 2.4 to 60.0</td>
<td>Mass flow of cooling fluid</td>
<td>0.04 to 0.54 L/min</td>
</tr>
</tbody>
</table>

If $R$ is considered as any function of independent linear parameters as in Eq. 11.

$$R = f(p_1, p_2, p_3, \ldots p_n)$$ (11)

Then the absolute uncertainty of function $R$ can be calculated as follows [53]:

$$\delta R = \sqrt{\left( \frac{\partial R}{\partial p_1} \delta p_1 \right)^2 + \left( \frac{\partial R}{\partial p_2} \delta p_2 \right)^2 + \cdots + \left( \frac{\partial R}{\partial p_n} \delta p_n \right)^2}$$ (12)

where $n$ is the total number of measured parameters. If the uncertainties of the parameters are independent and the absolute uncertainty divided by the function $R$, then the absolute uncertainty is converted to relative (fractional) uncertainty as shown in Eq. 13.

$$\frac{\delta R}{R} = \sqrt{\left( \frac{\delta p_1}{p_1} \right)^2 + \left( \frac{\delta p_2}{p_2} \right)^2 + \cdots + \left( \frac{\delta p_n}{p_n} \right)^2}$$ (13)
Based on Eq. 13, the uncertainties for electrical and thermal efficiencies were calculated from Eqs. 2, 4, and 8 and the values are shown in Table 3.

Table 3. Relative Uncertainties for irradiance, electrical and thermal efficiencies.

<table>
<thead>
<tr>
<th>$\delta G/G$</th>
<th>$\delta \eta_{elec}/\eta_{elec}$</th>
<th>$\delta \eta_{th}/\eta_{th}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$f(G)$ From measurement $\pm 0.0057$</td>
<td>$f(G, P_{MPP})$ From Eq. (2) $\pm 0.014$</td>
<td>$f(G, \dot{m}<em>{water}, T</em>{outlet}, T_{inlet})$ From Eqs. (4) and (8) $\pm 0.02$</td>
</tr>
</tbody>
</table>

2.4 Numerical modeling and simulations

3-Dimensional (3-D) numerical simulations were utilized to compute the thermal and hydraulic behaviors of the PV/T system. Table 4 shows the physical and thermal properties details of the PV module utilized in these simulations [54].

Table 4. Structural details of the PV module used in the simulations [54].
Figure 2 shows the steady-state energy balance for the PV/T system used in this study. The general form for energy balance can be presented as in Eq. 14.

\[
\frac{dQ}{dt} = \dot{Q}_{in} - \dot{Q}_{out}
\]  
(14)

For steady state condition, the previous energy balance equation becomes

\[
\dot{Q}_{in} = \dot{Q}_{out} \Rightarrow \dot{Q}_{in} = \dot{Q}_{elec} + \dot{Q}_{th} + \dot{Q}_{loss}
\]  
(15)

where \(\dot{Q}_{in}\) is the incidence solar irradiance (AG) on the top surface of the PV/T system, \(\dot{Q}_{loss}\) is the rate of heat losses from the PV/T system by convection and radiation which are calculated by Eqs. 16 and 17, respectively.

\[
\dot{Q}_{conv} = h A_c (T_{p,m} - T_a)
\]  
(16)

\[
\dot{Q}_{rad} = \sigma \varepsilon (T_{p,m} + T_{Sky})(T_{p,m}^2 + T_{Sky}^2)A_c (T_{p,m} - T_{sky})
\]  
(17)

where \(h\) is the heat transfer coefficient in (W/m².K), for this condition, \(h\) was used based on the approximation proposed by Watmuff et al. 1977 [55].

\[
h = 2.8 + 3 \times V
\]  
(18)

where \(V\) is the speed of wind in (m/s). This approximation is used after considering the variation

on the speed is less than 4 (m/s). \(\sigma\) is Stefan Boltzmann constant which equal to \(5.67 \times 10^{-8}\) W/m\(^2\)K\(^4\), \(\varepsilon\) is the emissivity of the PV/T surface and \(T_{sky} = 0.05527^{1.5}\) is the sky temperature [43]. The solar PV system was cooled from the backside, the copper channel dimensions are 0.0127 m \(\times\) 0.00635 m.

![Figure 2. The energy balance for a PV/T system consists of eleven copper cooling channels.](image)

### 2.4.1 Geometry and mesh

The geometry was created in 3-D by DesignModeler software inside ANSYS 15. The geometry was split into several control volumes to solve for conservation equations. The hexahedral shaped elements were used for simulations because it has a high aspect ratio as shown in Figure
3. The mesh size was selected based on grid independent study. The mesh size was refined for the fluid flow inside the cooling channel, the size was 0.00071 m. However, the size for the mesh inside the PV module was 0.0032 m as shown in Figure 3. Different numbers of grids were tested and the average temperature at the middle of the top surface was selected for the grid independent study as shown in Figure 3. The numerical uncertainty in the fine-grid for this CFD simulation was estimated by 2.37% based on the study done by [56]. In order to reduce the time of computational and achieve the convergence quickly, only one cooling channel out of eleven channels is considered in the numerical simulation instead to discretized the whole geometry of the PV/T system (PV module and the thermal system which consist from eleven copper cooling channels).

**Figure 3:** (a) Effect of the number of grids on the temperature at the top of PV module (b) Cross
section along the stream wise direction with hexahedral elements shapes for PV/T model (c)

Computational domain of the PV/T numerical model with a copper cooling channel at the bottom with 270000 hexahedral elements.

2.4.2 Physical properties and boundary conditions

The equivalent thermo-physical properties for the structural details of the PV module were used as in [57] after assumed the PV module one homogeneous unit. The values of these thermo-physical properties were based on the information displayed in Table 4 and Figure 2, while the thermo-physical properties for copper channels and the working fluid were used from the ANSYS Fluent database. The solar irradiance received the top surface of the computational domain was treated as constant heat flux after considering the product of solar transmissivity and solar absorptivity ($\tau\alpha$) of the PV module 0.9 [58], these values of heat flux were 900 W/m$^2$, 700 W/m$^2$, and 550 W/m$^2$ at different times of a typical day in April as shown in [48]. Both inlet and outlet boundary conditions were applied to the inlet and outlet positions of the copper cooling channel, respectively; four inlet water velocity values were simulated based on 0.4, 1.4, 3.4, and 5.4 (L/min) as the total mass flow rate in all eleven channels.

The convective heat transfer boundary condition was applied at the upper and lower side edges of the PV/T numerical model, as well as at the bottom side of the PV/T numerical model (PV module part) as shown in Figure 4. Two different thermal boundary conditions were applied on both sides (left and right) of the PV/T numerical model based on the position of the cooling channel as mentioned before. The symmetric boundary condition was used for the cooling
channel located in the middle of the PV module, while both symmetric and convective thermal boundaries condition were used for the cooling channel located at the left and right sides of the PV module. It is worth mentioning that the insulation thermal condition was applied to the copper cooling channel walls. The details of the boundary conditions for each type of PV/T model are presented in Table 5 and Figure 4.

Table 5. Type of boundary condition for three different locations of PV/T numerical model.

<table>
<thead>
<tr>
<th>Location of PV/T system</th>
<th>Type of boundary condition for different locations of PV/T numerical model</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Right side</td>
</tr>
<tr>
<td>Top of PV module</td>
<td>Constant heat flux (500, 700, and 900 W/m$^2$)</td>
</tr>
<tr>
<td>Right side of PV module</td>
<td>Convection heat transfer</td>
</tr>
<tr>
<td>Left side of PV module</td>
<td>Symmetry</td>
</tr>
<tr>
<td>Bottom side of PV module</td>
<td>Convection and radiation heat transfer</td>
</tr>
<tr>
<td>Upper side edge of PV module</td>
<td>Convection and radiation heat transfer</td>
</tr>
<tr>
<td>Lower side edge of PV module</td>
<td>Convection and radiation heat transfer</td>
</tr>
<tr>
<td>Inlet of copper channel</td>
<td>Constant velocity temperature, kinetic energy and dissipation rate</td>
</tr>
<tr>
<td>Outlet of copper channel</td>
<td>Pressure outlet</td>
</tr>
<tr>
<td>Inner walls of copper channel</td>
<td>No slip for velocity</td>
</tr>
<tr>
<td>Outer wall of copper channel</td>
<td>Thermal insulation</td>
</tr>
</tbody>
</table>
Figure 4. Boundary conditions for three different locations of PV/T model (a) left (b) middle (c) right.

2.4.3 Governing equations and mathematical model

ANSYS Fluent was used the finite volume method to solve the steady-state governing equations for the PV/T numerical model as shown in Table 6.
Table 6. Steady-state governing equations for the $k$-$\varepsilon$ turbulence model.

$$
\left\{ \frac{\partial}{\partial x} (\rho u \phi) + \frac{\partial}{\partial y} (\rho v \phi) + \frac{\partial}{\partial z} (\rho w \phi) \right\} = \frac{\partial}{\partial x} \left( \Gamma_\phi \frac{\partial \phi}{\partial x} \right) + \frac{\partial}{\partial y} \left( \Gamma_\phi \frac{\partial \phi}{\partial y} \right) + \frac{\partial}{\partial z} \left( \Gamma_\phi \frac{\partial \phi}{\partial z} \right) + S_{\phi}
$$

<table>
<thead>
<tr>
<th>Equation</th>
<th>$\phi$</th>
<th>$\Gamma_\phi$</th>
<th>$S_{\phi}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Continuity</td>
<td>1</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>$U$ momentum</td>
<td>$u$</td>
<td>$\mu + \mu_t$</td>
<td>$-\frac{\partial p}{\partial x} + \frac{\partial}{\partial x} \left( \Gamma_\phi \frac{\partial u}{\partial x} \right) + \frac{\partial}{\partial y} \left( \Gamma_\phi \frac{\partial v}{\partial x} \right) + \frac{\partial}{\partial z} \left( \Gamma_\phi \frac{\partial w}{\partial x} \right)$</td>
</tr>
<tr>
<td>$V$ momentum</td>
<td>$v$</td>
<td>$\mu + \mu_t$</td>
<td>$-\frac{\partial p}{\partial y} + \frac{\partial}{\partial x} \left( \Gamma_\phi \frac{\partial u}{\partial y} \right) + \frac{\partial}{\partial y} \left( \Gamma_\phi \frac{\partial v}{\partial y} \right) + \frac{\partial}{\partial z} \left( \Gamma_\phi \frac{\partial w}{\partial y} \right)$</td>
</tr>
<tr>
<td>$W$ momentum</td>
<td>$w$</td>
<td>$\mu + \mu_t$</td>
<td>$-\frac{\partial p}{\partial z} + \frac{\partial}{\partial x} \left( \Gamma_\phi \frac{\partial u}{\partial z} \right) + \frac{\partial}{\partial y} \left( \Gamma_\phi \frac{\partial v}{\partial z} \right) + \frac{\partial}{\partial z} \left( \Gamma_\phi \frac{\partial w}{\partial z} \right)$</td>
</tr>
<tr>
<td>Temperature</td>
<td>$T$</td>
<td>$\mu/\Pr + \mu_t/Pr_t$</td>
<td>0</td>
</tr>
<tr>
<td>Turbulent kinetic energy</td>
<td>$k$</td>
<td>$\mu + \mu_t/\sigma_k$</td>
<td>$G_k - \rho \varepsilon$</td>
</tr>
<tr>
<td>Dissipation rate</td>
<td>$\varepsilon$</td>
<td>$\mu + \mu_t/\sigma_\varepsilon$</td>
<td>$C_{1\varepsilon} \frac{\varepsilon}{k} G_k - \rho C_{2\varepsilon} \frac{\varepsilon^2}{k}$</td>
</tr>
</tbody>
</table>

$G_k$ is the generation of turbulence kinetic energy due to the mean velocity gradients and is given by Eq. 19.

$$
G_k = -\rho \overline{u_i' u_j'} \frac{\partial u_j}{\partial x_i}
$$

(19)

The variables $\sigma_k$ and $\sigma_\varepsilon$ are the turbulent Prandtl numbers for $k$ and $\varepsilon$. $C_{1\varepsilon}$ and $C_{2\varepsilon}$ are constants. The values of $\sigma_k$, $\sigma_\varepsilon$, $C_{1\varepsilon}$, and $C_{2\varepsilon}$ were 1, 1.3, 1.44, and 1.92, respectively. The
turbulent viscosity is calculated by combining $k$ and $\varepsilon$ as in Eq. 20.

$$\mu_t = \rho C_{\mu} \frac{k^2}{\varepsilon}$$  \hspace{1cm} (20)

The modeling constants $C_{\mu}$ value is 0.09. Both mass and Navier–Stokes equations were used to solve the incompressible flow field for the $k$-$\varepsilon$ turbulence model inside the copper cooling channel, while the energy equation was used to solve the temperature fields for the flow field inside the copper cooling channel, copper channel walls and the PV module. The convergence criteria for mass, momentum, and energy equations were $10^{-4}$, $10^{-6}$, and $10^{-7}$, respectively, these convergence criteria achieved after 7 minutes. The outlet temperature was evaluated based on the area average weight of the outlet of the cooling channel as shown in Eq. 21.

$$T_{out} = \frac{1}{\Delta A} \int T_{out} \, dA$$  \hspace{1cm} (21)

After the outlet temperature of cooling fluid was evaluated, Eq. 4 was used to calculate the thermal energy for the PV/T numerical model for the two cooling channels at the right and left (symmetric-convection) as well as the nine cooling channels at the middle (symmetric-symmetric) of PV/T system. Figure 5 shows the diagram for all procedures needed for the CFD of the PV/T system numerical simulations in this study.
3. Results and Discussion

3.1 Weather conditions

Figures 6 (a) and (b) display the ambient temperature, cell temperature, and the irradiance for both PV and PV/T modules during a typical day in April for Sharjah city in UAE. All the temperature curves in Figure 6 (a) follow the natural distribution of the ambient temperature during daylight. These three temperatures increase with time and reach a maximum values at around noon. These maximum temperature values for both PV/T and PV modules are 45 and
58°C, respectively, at maximum ambient temperature of 40°C. Then the temperatures decrease gradually until sunset. On the other hand, Figure 6 (b) shows that the irradiance for both PV and PV/T modules reaches maximum values of 916 and 898 W/m², respectively, at the solar noon.
Figure 6: The measuring parameters for PV and PV/T modules during a typical day of April in UAE (a) Ambient temperature and cell temperatures for PV and PV/T (b) Irradiance falls on PV and PV/T modules.

3.2 Electrical characteristic for the PV and PV/T systems

The electrical characteristics of the PV and the PV/T systems were measured using the profiTest PV analyzer device under three values of irradiance namely at 12:30 PM (900 W/m²) as shown in Figure 7 (a). It is clear from this figure that the PV/T module has a higher open-circuit voltage value of 20.34 V compared to the PV module value of 19.12 V. Whereas the values for the short circuit current were 6.25 A and 6.11 A for the PV/T and PV modules, respectively. The PV/T module shows a maximum power point (MPP) value of 82.97 W, the MPP for the PV/T is higher than the value of MPP for the PV module by 10 W. Figure 6 shows the measurements of electrical efficiencies for the PV/T and PV modules under different values of irradiance measured on the same working day in April. These efficiencies decrease linearly as the PV cell temperature increases as illustrated in Figure 7 (b). It is evident from Figure 6 that the minimum and maximum measurement electrical efficiencies for the PV/T module were 10.26 % and 12.5 %, respectively. On the other hand, the minimum and maximum measurement electrical efficiencies for the PV module were 10.23 % and 12.5, respectively. It is clear that there was no difference between the upper and lower limits of the electrical efficiencies and that is mainly due to the narrow range of the cell temperatures of the PV/T module (37.22 – 44.95°C). This makes the cooling system for the PV/T module more effective compared to the PV module without the cooling where the cell temperature ranges between 37.3 and 58.06°C. This difference in cell
temperature causes the 10 W increase in the MPP as aforementioned. The drop in the cell temperature enhances electrical efficiency, especially under hot climate weather conditions. In other words, the cell temperature for the PV/T was very close to the nominal operating cell temperature (NOCT) or the standard operating conditions (SOC), which allows the PV/T system to operate at a higher electrical efficiency compared to the PV system. The latter works at a cell temperature far away from the SOC temperature. The cooling system extracted the waste heat during the energy conversion process. Furthermore, the cooling system will enhance the overall efficiency of PV/T by recovery this wasted thermal energy and make the system more sustainable.

![IV PV/T and IV PV](image)
Figure 7: The electrical performance for PV and PV/T system during a typical day in April in UAE (a) The IV and power curves (b) Electrical efficiency.

3.3 Thermal characteristics of the PV/T system

3.3.1 Two-dimensional temperature distribution

The two-dimensional temperature distribution for PV/T system along the cooling channel (at the inlet, middle, and outlet positions) is displayed in Figure 8. As shown in Figure 8 (a), the value of the highest temperature was 342 K which was observed on the top surface in the middle of the PV/T module. This was when the symmetrical boundary condition applied on both sides in the numerical model. However, the lowest temperature was 311 K and it was at the inlet of the
cooling channel. The temperature on the top surface of the PV/T module for the symmetrical boundary condition decreases along the cooling channel from inlet to outlet. The range of the temperatures on the top surface were 311 to 330.1 K, 313.4 to 342 K, and 315.8 to 334.8 K for the inlet, middle, and outlet location of the cooling channel, respectively. While Figure 8 (b) and (c) show the two-dimensional temperature distribution when the symmetrical and convective boundaries conditions applied on both sides of the numerical model. The highest temperature was 337.9 K and it was observed in the middle of the PV/T module. The value of temperature for this boundary condition is lower than the value when the symmetrical thermal boundary condition applied on both sides of the numerical model. By similarity with symmetrical boundary conditions, the temperature at the top side of the PV/T module decreases along the cooling channel from inlet to outlet. The ranges of temperature in the inlet, middle, and outlet locations on the top surface were 311 to 327.6 K, 311 to 337.9 K, and 311 to 329.6 K, respectively. Figures 8 (a), (b), and (c) show also that the top side of the PV/T module has the highest value of the temperature where the constant heat flux is applied, this value decreases to the lowest value when reaches the bottom of the copper channel of the cooling system.
Figure 8: Temperature contour plot for different boundary condition (a) symmetric-symmetric along the middle of PV module length (b) symmetric-convection conditions along the right edge of the PV module length (c) symmetric-convection conditions along the left edge of the PV module length at different location (1) inlet (2) middle (3) outlet.
3.3.2 Useful thermal energy from the PV/T system

Figure 9 (a) shows the useful thermal energy of the PV/T that was absorbed by water under different values of irradiance (550, 700, and 900 W/m²). The absorbed thermal energy increases as both irradiance and mass flow rates increase from 500 to 900 W/m² and from 0.4 to 5.4 L/min, respectively. Corresponding to what mentioned in Figure 8, the thermal energy is higher when symmetrical boundary conditions applied on both sides of the PV/T module for the channels located in the middle of the PV/T module. It is worth it to point out that nine channels out of eleven have symmetrical thermal boundary conditions (Sym. - Sym. B.C.) on both sides of the PV/T numerical model. While the channel on the lift side edge of the PV/T module has convection and symmetrical (Conv. - Sym. B.C.) thermal boundary conditions on the left and right sides edges of the PV/T numerical model, respectively, and vice versa for the right side edge of the PV/T module. The thermal energy variation with all values of mass flow rates for different thermal boundary conditions at 700 W/m² is shown in Figure 9 (b). The thermal energy for both boundary conditions increases as the mass flow rates increase from 0.4 to 5.4 L/min. The big variation of thermal energy with the mass flow rates is clearly obtained for the channel in the middle of the PV/T module at the low mass flow rate as compared to the two channels on the left and right edges of the PV/T module. The total thermal energy for the PV/T model will follow the trend of thermal energy for symmetrical- symmetric boundary conditions, that because this boundary condition applied for the majority of channels (9 channel out of 11).
**Figures 9:** Thermal energy under different thermal boundary conditions (a) different irradiance values along the day (b) different mass flow rates values at 700 W/m$^2$. 
3.3.3 Three-dimensional temperature distribution

Figure 10 shows the three-dimensional temperature distribution for the PV/T module. The temperature readings have the highest value at the upper surface where the PV/T module exposed to constant irradiance (heat flux). The temperature on the top surface increases along the direction of the cooling from the inlet at 334.8 K to 342 K in the middle then tends to decrease again to 337.2 K at the outlet. The figure shows also the effect of symmetric-symmetric and symmetric convection boundary conditions on the temperature values. All the edges around the top side of the PV/T module, especially at the corners, where the symmetric convection boundary conditions applied have the lowest temperatures. The temperature of the PV/T module decreases from 334.8 - 342 K at the top surface to around 327.7 K at the middle plane between the top and bottom surfaces. The temperature reaches the lowest value of 311 K at the bottom surface where the water cooling channels installed.
Figure 10: Three-dimensional temperature distribution in (K) for PV/T system for a typical day in April in UAE.

3.3.4 Thermal efficiency of the PV/T system

The thermal efficiency under different irradiance and mass flow rates are displayed in Figure 11 (a) and (b). Evidently, the thermal efficiency increases as the irradiance increase under the same mass flow rate, the mass flow rate 5.4 L/min has a higher thermal efficiency value than the mass flow rate 0.4 L/min, where the maximum $\eta_{th}$ obtained at 900 (W/m²) as displayed in Figure 11 (a). Figure 11 (b) shows the variation of the thermal efficiency with the mass flow rate. For 900 W/m², as the mass flow rate increases from 0.4 to 1.4 L/min the thermal efficiency increases from 61% to 66%. After that, it increases slightly from 66% to 69% as the mass flow rate increases from 1.4 to 5.4 L/min. It is noteworthy to mention that the feasible value of the mass flow rate in this study is 1.4 L/min. The feasible value of the mass flow rate is crucial for selecting the capacity of the pump which is an essential factor for the cost-effectiveness of the PV/T cooling system.
Figures 11: Thermal efficiency for a typical day of April in UAE at (a) different irradiance values along the day (b) different values of mass flow rates.
3.3.5 Validation and verification of the current PV/T model

The results of the thermal efficiency for this work were compared with several studies in the literature. For example, the numerical simulation of this work was performed for three different values of irradiance (500, 700, and 900 W/m²) and four different mass flow rates (0.4, 1.4, 3.4, and 5.4 L/min). The removal factor $F_R(\tau\alpha)$ is the maximum efficiency that the PV/T module can achieve when $\Delta T/G$ equals zero, i.e. intersection of the vertical axis for $\eta_{th}$ versus $\Delta T/G$. The $F_R(\tau\alpha)$ computed from this numerical model was very close to the value reported in Sandnes et al. 2002 [59] at 5.4 (L/min). Moreover, the $F_RU_L$ values have small differences due to the difference in the area of the PV module, evident from Figure 12 (a) and Table 7. Furthermore, the values of $F_R(\tau\alpha)$ and $F_RU_L$ reported in Sandnes et al. 2002 [59] depend on the weather conditions. On the other hand, the values of $F_R(\tau\alpha)$ and $F_RU_L$ computed by the developed model at a low mass flow rate (0.4 and 1.4 L/min) were compared to the values reported in Tiwari et al. 2006 [58], Zondag et al. 2003 and 2002 [60,61] and Tripanagnostopoulos et al. 2002 [62], see Figure 12 (b) and Table 2. However, the small difference in the values of $F_RU_L$ is due to the difference in the PV module area and the high thermal conductivity of the copper cooling channel. It is evident from Table 2 that the values of $F_RU_L$ for this work were high at low mass flow rates and were low at high mass flow rates.

Table 7 shows a summary of the results reported in the literature [58, 59 - 62] for $F_R(\tau\alpha)$ and $F_RU_L$ compared to the results obtained in this work for different PV/T module areas. The results reported in the literature were based on experimental work or numerical models of one, two, or three dimensional. Figure 12, on the other hand, shows a comparison between the thermal efficiency in this study and various studies in the literature under varying values of $\Delta T/G$ for
high and low mass flow rates. It is clear from Figure 9 that the thermal efficiency is inversely
proportional to $\Delta T/G$ for all studies. It is worth it to mention that the highest thermal efficiency
obtained at different values of the mass flow rate [63-69], and the covered or glazed PV/T has
less thermal efficiency compared with the uncovered or unglazed [59, 60]. Moreover, in addition
to mass flow rate value, the highest value of thermal efficiency for the PV/T system depends on
many parameters such as ambient, operating conditions, the spacing between the channels, and
the area of PV/T module as shown in Eqs. 6 and 7.

**Table 7.** Summary of thermal efficiency parameters (intersection $FR(\tau\alpha)$, and slope $FRUL$) for
the current work and other studies in the literature.

<table>
<thead>
<tr>
<th>$\eta_{th}$ at $\Delta T/G = 0$ (%) or $FR(\tau\alpha)/average$</th>
<th>$FRUL$ (W/m².C)</th>
<th>Area (m²)</th>
<th>Mass flow rate (Unit)</th>
<th>Irradiance (W/m²)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.70</td>
<td>8.10</td>
<td>0.32</td>
<td>-</td>
<td>-</td>
<td>[59]</td>
</tr>
<tr>
<td>0.6825</td>
<td>6.89</td>
<td>0.784</td>
<td>5.4 L/min</td>
<td>-</td>
<td>[This study]</td>
</tr>
<tr>
<td>0.72</td>
<td>8.50</td>
<td>0.32</td>
<td>-</td>
<td>-</td>
<td>[59]</td>
</tr>
<tr>
<td>0.6825</td>
<td>6.89</td>
<td>0.784</td>
<td>5.4 L/min</td>
<td>-</td>
<td>[This study]</td>
</tr>
<tr>
<td>0.58 (m PV off)</td>
<td>5.2</td>
<td>0.94</td>
<td>76 kg/m² h</td>
<td>800</td>
<td>[60]</td>
</tr>
<tr>
<td>0.63 (2D PV off)</td>
<td>4.8</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.6575</td>
<td>7.24</td>
<td>0.784</td>
<td>1.4 L/min</td>
<td>550, 700</td>
<td>[This study]</td>
</tr>
<tr>
<td>Parameter</td>
<td>Value</td>
<td>1.4 L/min</td>
<td>0.02 kg/s</td>
<td>800</td>
<td>Reference</td>
</tr>
<tr>
<td>-----------</td>
<td>-------</td>
<td>-----------</td>
<td>-----------</td>
<td>-----</td>
<td>-----------</td>
</tr>
<tr>
<td>0.53 (m PV on)</td>
<td>0.55 (2D PV on)</td>
<td>5.2</td>
<td>4.4</td>
<td>and 900</td>
<td>[61]</td>
</tr>
<tr>
<td>0.625 / 0.56 (1D)</td>
<td>0.62 / 0.535 (2D)</td>
<td>4.8</td>
<td>7.24</td>
<td>0.94</td>
<td>0.02 kg/s</td>
</tr>
<tr>
<td>0.59 (3D)</td>
<td>0.6575</td>
<td>7.24</td>
<td>0.784</td>
<td>1.4 L/min</td>
<td>550, 700 and 900</td>
</tr>
<tr>
<td>0.71</td>
<td>9.04</td>
<td>0.4</td>
<td>0.02 kg/s</td>
<td>850.910, 898</td>
<td>[22]</td>
</tr>
<tr>
<td>0.6575</td>
<td>7.24</td>
<td>0.784</td>
<td>1.4 L/min</td>
<td>550, 700 and 900</td>
<td>[This study]</td>
</tr>
<tr>
<td>77.25</td>
<td>60 – 65</td>
<td>0.648</td>
<td>45 kg</td>
<td>Winter</td>
<td>[58]</td>
</tr>
<tr>
<td>60.3 – 65.8</td>
<td>7.27</td>
<td>0.784</td>
<td>0.4 – 1.4 L/min</td>
<td>Summer</td>
<td>[This study]</td>
</tr>
</tbody>
</table>
Figures 12: Comparison of experimental and numerical thermal efficiency versus $\Delta T/G$ (a) at 5.4 L/min with work done by [39,44] (b) at 0.4 & 1.4 L/min with work done by [45,46].
4. Conclusions

Novel 3-D numerical simulations were performed under different irradiance conditions and mass flow rates to study the performance of the PV/T system. The computational time for numerical simulation was reduced by applying different thermal boundary conditions on both sides of the novel PV/T numerical model. The number of elements for the numerical simulations conducted in the literature was higher than the current study by 5 to 12 times which lead to an increase in the computational time. The current model is much simpler and more efficient with less computational time. The results demonstrate that the middle of the PV/T module has the highest temperature where the symmetrical boundary conditions were applied on both sides of the PV/T numerical model. Several factors, namely, the overall heat transfer coefficient, the mass flow rate, the area of PV module, the specific heat, and the ambient conditions (irradiance, ambient, and fluid cooling temperature) affect the thermal efficiency of the PV/T system. A low value of $(\Delta T/G)$ has the highest thermal efficiency where the irradiance and the temperature difference between the ambient temperature and the inlet temperature of the cooling fluid were very high and very low, respectively. The novel numerical model shows that these results were in a decent concurrence with the results reported in the literature. The overall efficiency enhanced not only by increasing the electrical efficiency from 1 to 1.5% but also by utilizing the thermal energy for some applications such as solar heating and cooling systems. As in solar liquid desiccant cooling system for trigeneration applications (cooling, heating, and power generation), solar desiccant wheel evaporative cooling system (SDWECS), adsorption gas heat pump, and domestic hot water. There are several limitations for this model such as the cooling channels were distributed
in a symmetrical configuration, the cooling channels should be rectangular and fixed at the backside of the PV module, the contact region between the PV module and the cooling channels was assumed to be perfect without any resistance, the flow is incompressible and turbulent, and the variation on the wind speed is less than 4 m/s.

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References


Highlights

- The thermal performance of a PV/T module was evaluated by a novel numerical model for a hot climate region.
- The computational time was reduced by applying different thermal boundary conditions on both sides of the PV/T numerical model.
- Three-dimensional temperature distribution of the PV/T module was presented.
- The thermal energy was validated using different values of mass flow rates.
Tareq Salameh: Conceptualization, Project administration, Methodology, Funding acquisition, Supervision, Writing - review & editing. Muhammad Tawalbeh: Investigation, Validation, Methodology, Formal analysis, Data curation, Writing - original draft. Adel Juaidi: Investigation, Methodology, Formal analysis, Writing - review & editing. Ramez Abdallah: Investigation, Methodology, Writing - review & editing. Abdul-Kadir Hamid: Project administration, Funding acquisition, Supervision, review & editing.
Declaration of interests

☒ The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

☐ The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: